

Clase 66 9 diciembre 2020

Título de la nota

09/12/2020

$$\bar{V}^3 + \bar{V}^2 \left[2c - b - \frac{RT}{p} \right] + \bar{V} \left[c^2 - \frac{2RcT}{p} - 2cb + \frac{a}{pT} \right] - \left[c^2 \left(b + \frac{RT}{p} \right) + \frac{ab}{pT} \right] = 0$$

$$\left(\frac{L}{\text{mol}} \right)^3$$

$$+ \left(\frac{L}{\text{mol}} \right)^2 \left[\frac{L}{\text{mol}} - \frac{L}{\text{mol}} - \frac{L}{\text{mol}} \right]$$

$$\frac{L}{\text{mol}} \left[\left(\frac{L}{\text{mol}} \right)^2 - \frac{(\cancel{\text{atm L/mol}} \cancel{\text{K}})}{\cancel{\text{atm}}} \right] = \left(\frac{L}{\text{mol}} \right)^3$$

$$\left(\frac{L}{\text{mol}} \right)^2 \left[\left(\frac{L}{\text{mol}} + \frac{L}{\text{mol}} \right) + \frac{(\cancel{\text{atm L}^2 \cancel{\text{K}}}) \left(\frac{L}{\text{mol}} \right)}{\cancel{\text{atm}} \cancel{\text{K}}} \right]$$

$$\left[\frac{L^3}{\text{mol}^3} + \frac{L^3}{\text{mol}^3} \right]$$

$$\bar{V}^3 + \bar{V}^2 \left[2c - b - \frac{RT}{p} \right] + \bar{V} \left[c^2 - \frac{2RcT}{p} - 2cb + \frac{a}{pT} \right] - \left[c^2 \left(b + \frac{RT}{p} \right) + \frac{ab}{pT} \right] = 0$$

Redlich - Kwong (1949)

$$p = \frac{RT}{(\bar{V}-b)} \left[\frac{a}{(\bar{V}^2 + \bar{V}b)T^{0.5}} \right]$$

Despejar T

$$T^3 - T \left[\frac{p^2 (\bar{v} - b)^2}{R^2} \right] - \frac{a^2 (\bar{v} - b)^2}{R^2 (\bar{v}^2 + \bar{v}b)^2} = 0$$

$$p = \frac{RT}{\bar{v} - b} - \frac{a}{(\bar{v}^2 + \bar{v}b) T^{0.5}}$$

$$p + \frac{a}{(\bar{v}^2 + \bar{v}b) T^{0.5}} = \frac{RT}{(\bar{v} - b)}$$

$$\frac{\left\{ \left[p (\bar{v}^2 + \bar{v}b) T^{0.5} \right] + a \right\} (\bar{v} - b)}{(\bar{v}^2 + \bar{v}b) T^{0.5}} = RT$$

$$\frac{\left\{ \left[p(\bar{v}^2 + \bar{v}b) T^{0.5} \right] + a \right\} (\bar{v} - b)}{(\bar{v}^2 + \bar{v}b) T^{0.5}} = RT$$

$$\frac{\left[\bar{p}(\bar{v}^2 + \bar{v}b) T^{0.5} \right] (\bar{v} - b) + a (\bar{v} - b)}{(\bar{v}^2 + \bar{v}b) T^{0.5}} = RT$$

$$\frac{\left[\bar{p}(\bar{v}^2 + \bar{v}b) T^{0.5} \right] (\bar{v} - b) + a (\bar{v} - b)}{(\bar{v}^2 + \bar{v}b)} = RT^{1.5}$$

$$\frac{\left[p(\bar{v}^2 + \bar{v}b) T^{0.5} \right] (\bar{v} - b) + a (\bar{v} - b)}{(\bar{v}^2 + \bar{v}b)} = R T^{1.5}$$

$$\left\{ T^{0.5} (p) (\bar{v} - b) + \frac{a (\bar{v} - b)}{(\bar{v}^2 + \bar{v}b)} = R T^{1.5} \right\}^2$$

$$T (p^2) (\bar{v} - b)^2 + \frac{a^2 (\bar{v} - b)^2}{(\bar{v}^2 + \bar{v}b)^2} = R^2 T^3$$

$$T^3 - T \left[\frac{p^2 (\bar{v} - b)^2}{R^2} \right] - \frac{a^2 (\bar{v} - b)^2}{R^2 (\bar{v}^2 + \bar{v}b)^2} = 0$$

$$T^3 - T \left[\frac{p^2 (\bar{v}-b)^2}{R^2} \right] - \frac{a^2 (\bar{v}-b)^2}{R^2 (\bar{v}^2 + \bar{v}b)^2} = 0$$

$$a = \frac{\text{atmL}^2 \text{K}^{0.5}}{\text{mol}^2} = \frac{0.4278 R^2 T_c^{2.5}}{p_c}$$

$$b = \frac{\text{L}}{\text{mol}} = \frac{0.0867 R T_c}{p_c}$$

$$T^3 - T \left[\frac{p^2 (\bar{v}-b)^2}{R^2} \right] - \frac{a^2 (\bar{v}-b)^2}{R^2 (\bar{v}^2 + \bar{v}b)^2} = 0$$

$$K^3 - K \left[\frac{\text{atm}^2 \left(\frac{\text{L}}{\text{mol}} \right)^2}{\left(\frac{\text{atmL}}{\text{molK}} \right)^2} \right] \therefore K^3 - K (K^2)$$

$$\frac{\left(\frac{\cancel{\text{atm}} \cancel{\text{L}}^2 \text{K}^{0.5}}{\cancel{\text{mol}}^2} \right)^2 \left(\frac{\cancel{\text{L}}}{\cancel{\text{mol}}} \right)^2}{\left(\frac{\cancel{\text{atm}} \cancel{\text{L}}}{\cancel{\text{mol}} \text{K}} \right)^2 \left[\left(\frac{\cancel{\text{L}}}{\cancel{\text{mol}}} \right)^2 \right]^2}$$

$$\frac{\text{K}}{\text{K}^2} = \text{K}^{-1}$$

Obtención de ecuación cúbica de la temperatura tipo Redlich-Kwong

Introducir los valores en las celdas de color amarillo

Tc (K)	126.1500
V (L/mol)	2.0000
pc (atm)	33.5000
p sistema (atm)	4.5750
a (atmL ² K ^{0.5} /mol ²)	15.3476
b (L/mol)	0.0268
R (atmL/molK)	0.082

Modelo 2

$$T^3 - T \left[\frac{p^2 (\bar{V} - b)^2}{R^2} \right] - \frac{a^2 (\bar{V} - b)^2}{R^2 (\bar{V}^2 + \bar{V}b)^2} = 0$$

T ³	T ²	T	Cte
1	0	-12120.1830	-8301.2018

T ideal (K) 111.5854

T real (K) 110.433

Resolución de la ecuación tipo AT³+BT²+CT+D=0

A=	1
B=	0
C=	-12120.1830
D=	-8301.2018

Expresión	4	decimales
-----------	---	-----------

	Real	Imaginaria	
T1=	110.433	0.000	+110.4326
T2=	-109.748	0.000	-109.7476
T3=	-0.685	0.000	-0.6849



Dr. Juan Carlos Vázquez Lira UNAM FES Zaragoza 2020

Con apoyo del programa UNAM-DGAPA-PAPIME PE-200419

$$\bar{V}^3 - \bar{V}^2 \left[\frac{RT}{p} \right] - \bar{V} \left[b^2 + \frac{bRT}{p} - \frac{a}{pT^{0.5}} \right] - \left[\frac{ab}{pT^{0.5}} \right] = 0$$

$$p = \frac{RT}{(\bar{V}-b)} - \left[\frac{a}{(\bar{V}^2 + \bar{V}b)T^{0.5}} \right]$$

$$\frac{\left[p(\bar{V}^2 + \bar{V}b)T^{0.5} + a \right] (\bar{V}-b)}{(\bar{V}^2 + \bar{V}b)T^{0.5}} = RT$$

$$\frac{\left[p(\bar{V}^2 + \bar{V}b)T^{0.5} \right] (\bar{V}-b) + a(\bar{V}-b)}{(\bar{V}^2 + \bar{V}b)T^{0.5}} = RT$$

$$\frac{[p(\bar{v}^2 + \bar{v}b)T^{0.5}](\bar{v}-b) + a(\bar{v}-b)}{T^{0.5}} = RT(\bar{v}^2 + \bar{v}b)$$

$$\frac{p(\bar{v}^3 + \bar{v}^2 b)T^{0.5} + p(\bar{v}^3 b + \bar{v}b^2)T^{0.5}}{pT^{0.5}} + \frac{a(\bar{v}-b)}{pT^{0.5}} = \frac{RT\bar{v}^2 + RT\bar{v}b}{p}$$

$$\bar{v}^3 + \bar{v}^2 b - \bar{v}^2 b - \bar{v}b^2 + \frac{a\bar{v}}{pT^{0.5}} - \frac{ab}{pT^{0.5}} = \frac{RT\bar{v}^2 + RT\bar{v}b}{p}$$

$$\bar{v}^3 - \bar{v}b^2 + \frac{\bar{v}a}{pT^{0.5}} - \frac{\bar{v}RTb}{p} - \frac{RT\bar{v}^2}{p} - \frac{ab}{pT^{0.5}} = 0$$

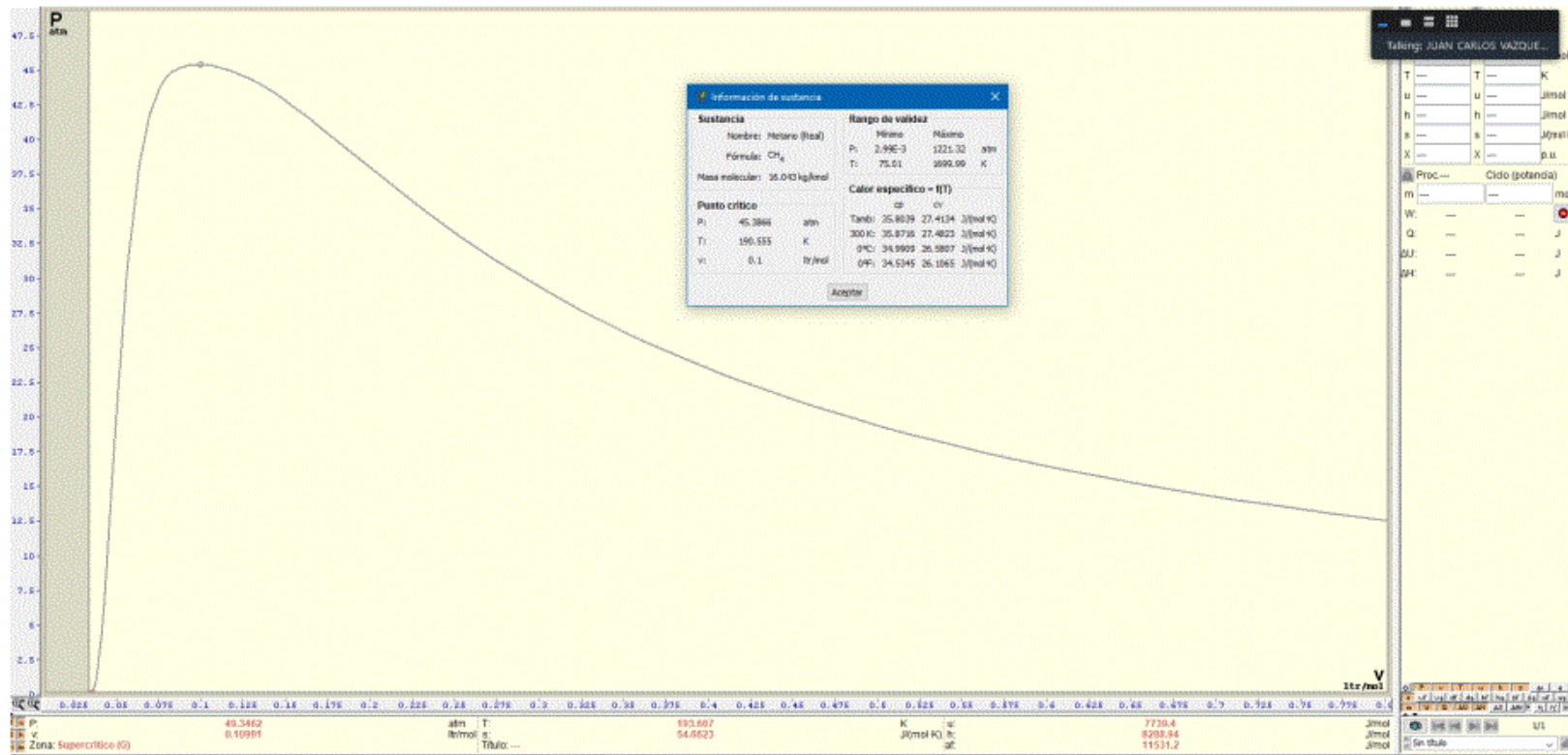
$$\bar{v}^3 - \bar{v}b^2 + \frac{\bar{v}a}{pT^{0.5}} - \frac{\bar{v}RTb}{P} - \frac{RT\bar{v}^2}{P} - \frac{ab}{pT^{0.5}} = 0$$

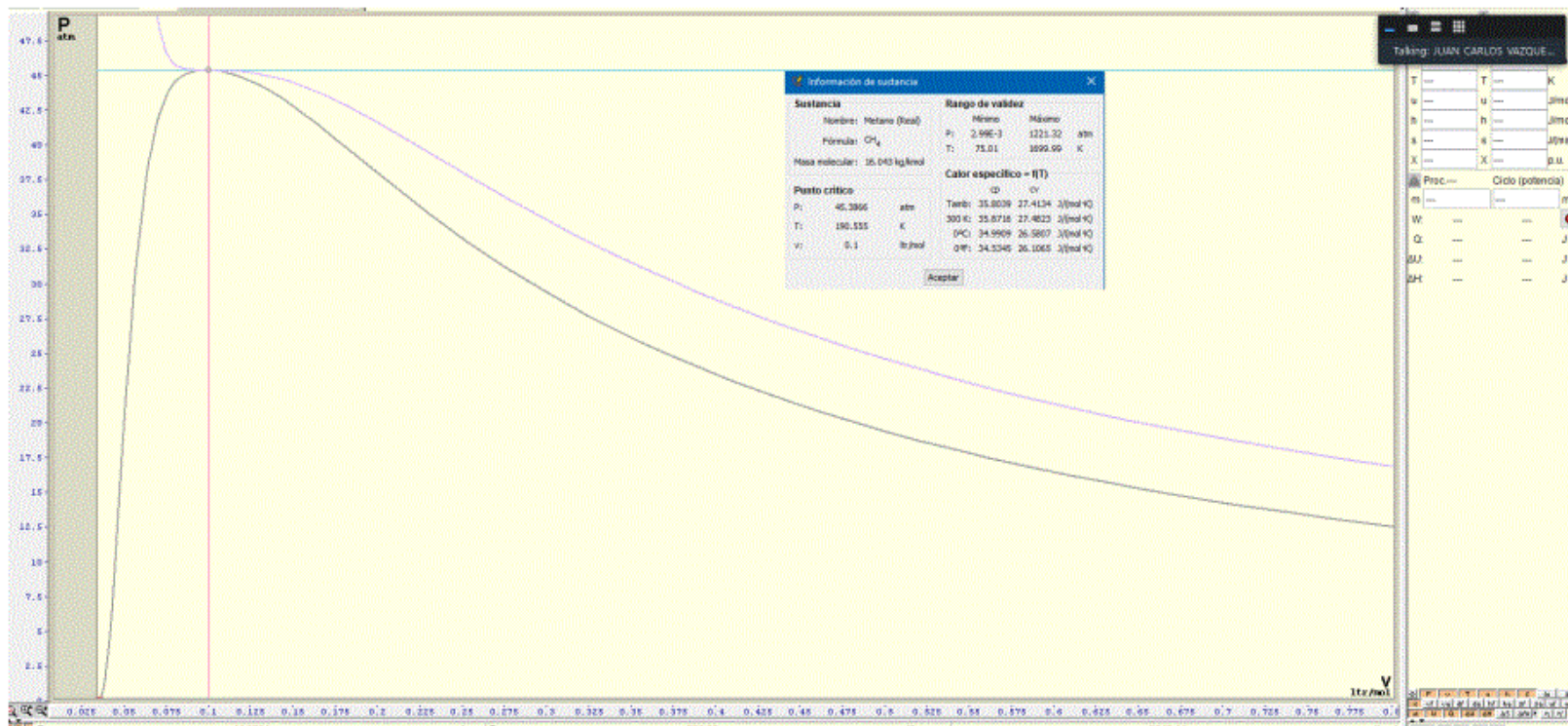
$$\bar{v}^3 - \bar{v}^2 \left(\frac{RT}{P} \right) - \bar{v} \left(b^2 + \frac{RTb}{P} - \frac{a}{pT^{0.5}} \right) - \frac{ab}{pT^{0.5}} = 0$$

$$\bar{v}^3 - \bar{v}^2 \left[\frac{RT}{P} \right] - \bar{v} \left[b^2 + \frac{bRT}{P} - \frac{a}{pT^{0.5}} \right] - \frac{ab}{pT^{0.5}} = 0$$

$$\left(\frac{L}{mol} \right)^3 - \left(\frac{L}{mol} \right)^2 \left(\frac{L}{mol} \right) - \frac{L}{mol} \left[\left(\frac{L}{mol} \right)^2 + \left(\frac{L}{mol} \right)^2 - \frac{atm L^2 K^{0.5}}{atm mol^2 K^{0.5}} \right] - \frac{atm L^2 K^{0.5}}{atm mol^2 K^{0.5}} = 0$$

$$\frac{\left(\frac{atm L^2 K^{0.5}}{mol^2} \right) \left(\frac{L}{mol} \right)}{atm K^{0.5}} = \left(\frac{L}{mol} \right)^3$$





Obtención de la presión de un gas con el modelo tipo Redlich-Kwong

Introducir los valores en las celdas de color amarillo

Tc (K)	190.56
V sistema (L/mol)	2.0000
pc (atm)	45.3866
a (atmL ² K ^{0.5} /mol ²)	31.7681
b (L/mol)	0.0298
R (atmL/molK)	0.082
T sistema(K)	250.00

Modelo

$$p = \frac{RT}{(\bar{V}-b)} - \left[\frac{a}{(\bar{V}^2 + \bar{V}b)T^{0.5}} \right]$$

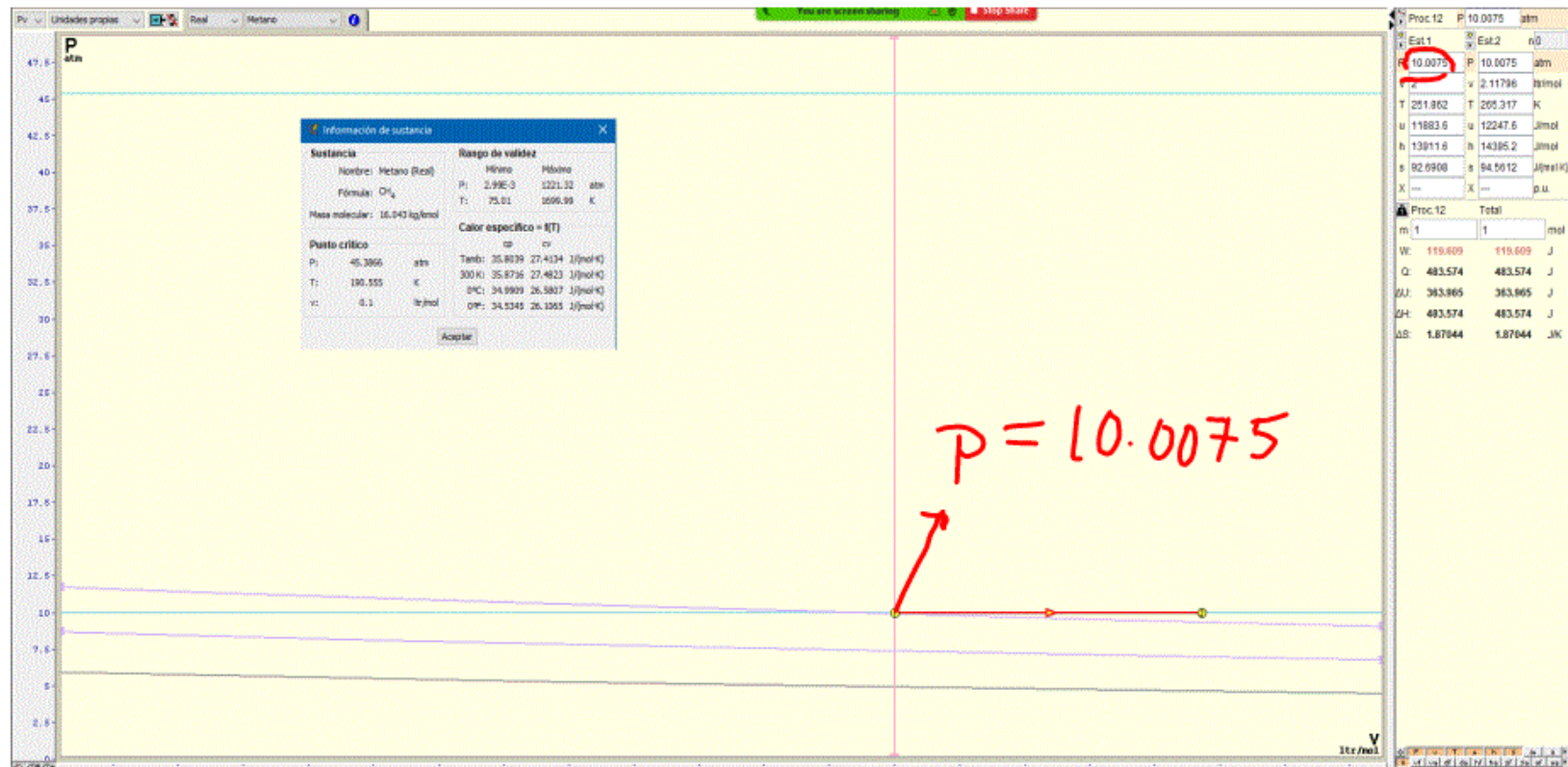


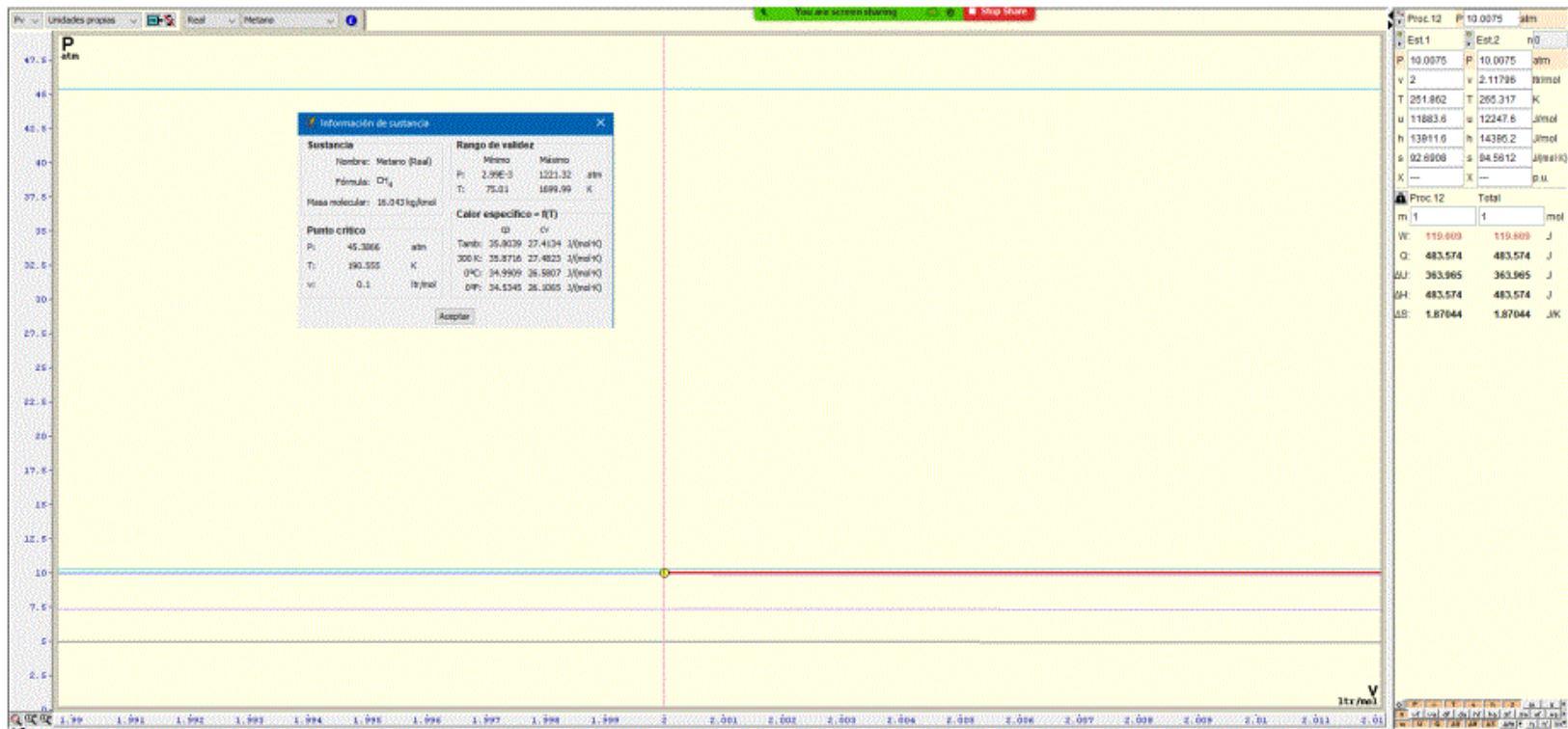
p ideal (atm)	10.2500
p real (atm)	9.9104

Dr. Juan Carlos Vázquez Lira UNAM FES Zaragoza 2020

Con apoyo del programa UNAM-DGAPA-PAPIME PE-200419







Obtención de la presión de un gas con el modelo tipo Clausius

Introducir los valores en las celdas de color amarillo

Tc (K)	190.56
V sistema(L/mol)	2.0000
pc (atm)	45.4000
a (atmL ² K/mol ²)	432.3653
b (L/mol)	0.0140
R (atmL/molK)	0.082
T sistema(K)	250.00
c (L/mol)	0.0291
Vc (L/mol)	0.1000

Modelo

$$P = \frac{RT}{(\bar{V}-b)} - \left[\frac{a}{(\bar{V}+c)^2 T} \right]$$



p ideal (atm)	10.2500
p real (atm)	9.9020

Dr. Juan Carlos Vázquez Lira UNAM FES Zaragoza 2020

Con apoyo del programa DGAPA-UNAM-PAPIME PE-200419

Volumen (L)	4.0000
Temperatura (K)	250.00
moles (n)	2.0000
a_M (atmL ² /mol ²)	2.2689
b_M (L/mol)	0.0430
R (atmL/molK)	0.082

p ideal (atm)	10.2500
p real (atm)	9.9081

Dr. Juan Carlos Vázquez Lira UNAM FES Zaragoza 2020

Con apoyo del programa UNAM-DGAPA-PAPIME PE-200419